

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Lecture 4

Dr. Manoj Kumar

Assistant Professor

Department of Mathematics

Institute of Applied Sciences and Humanities

GLA University Mathura-281406, India

Outline of Lecture 4

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

- **Graphic Presentations of Frequency Distributions.**

Graphic Presentations of Frequency Distributions

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

In this section we shall discuss how to present frequency distribution graphically. Graphs present data in a two-dimensional picture. On the horizontal axis, we show the values of the variable. On the vertical axis, we mark the frequencies of the classes shown on the horizontal axis.

A frequency distribution can be presented graphically in any of the following ways:

1. Histograms
2. Frequency Polygons
3. Frequency Curves
4. Ogives or Cumulative Frequency Curves

Graphic Presentations of Frequency Distributions

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

In this section we shall discuss how to present frequency distribution graphically. Graphs present data in a two-dimensional picture. On the horizontal axis, we show the values of the variable. On the vertical axis, we mark the frequencies of the classes shown on the horizontal axis. A frequency distribution can be presented graphically in any of the following ways:

1. Histograms
2. Frequency Polygons
3. Frequency Curves
4. Ogives or Cumulative Frequency Curves

Graphic Presentations of Frequency Distributions

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

In this section we shall discuss how to present frequency distribution graphically. Graphs present data in a two-dimensional picture. On the horizontal axis, we show the values of the variable. On the vertical axis, we mark the frequencies of the classes shown on the horizontal axis. A frequency distribution can be presented graphically in any of the following ways:

1. Histograms
2. Frequency Polygons
3. Frequency Curves
4. Ogives or Cumulative Frequency Curves

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

A histogram is the most widely used way of presenting a given frequency distribution graphically.

Example 1: Draw a histogram to represent the following data:

Daily wages (Rs.): 0-10 10-20 20-30 30-40 40-50 50-60

No. of Workers: 3 9 15 30 18 5

Solution: On the horizontal axis, we have shown the class intervals. On the vertical axis, we have marked the frequencies of the classes shown on the horizontal axis.

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

A histogram is the most widely used way of presenting a given frequency distribution graphically.

Example 1: Draw a histogram to represent the following data:

Daily wages (Rs.):	0-10	10-20	20-30	30-40	40-50	50-60
No. of Workers:	3	9	15	30	18	5

Solution: On the horizontal axis, we have shown the class intervals. On the vertical axis, we have marked the frequencies of the classes shown on the horizontal axis.

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

A histogram is the most widely used way of presenting a given frequency distribution graphically.

Example 1: Draw a histogram to represent the following data:

Daily wages (Rs.): 0-10 10-20 20-30 30-40 40-50 50-60

No. of Workers: 3 9 15 30 18 5

Solution: On the horizontal axis, we have shown the class intervals. On the vertical axis, we have marked the frequencies of the classes shown on the horizontal axis.

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

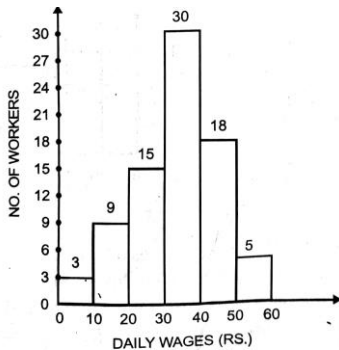


Fig. 1

1.jpg

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Example 2: Draw a histogram to represent the following data:

Mid-Value(X): 115 125 135 145 155 165

No. of Workers: 3 6 8 7 4 2

Hint: If the mid-values of various classes are given in place of class intervals then these must first be converted into classes.

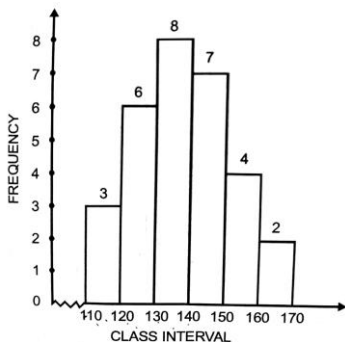


Fig. 2

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Example 2: Draw a histogram to represent the following data:

Mid-Value(X): 115 125 135 145 155 165

No. of Workers: 3 6 8 7 4 2

Hint: If the mid-values of various classes are given in place of class intervals then these must first be converted into classes.

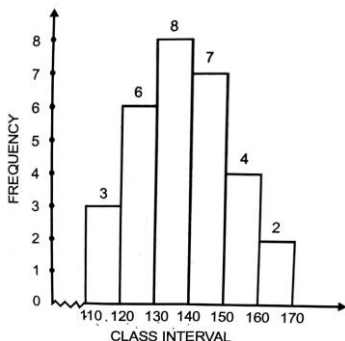


Fig. 2

Histograms

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Example 2: Draw a histogram to represent the following data:

Mid-Value(X): 115 125 135 145 155 165

No. of Workers: 3 6 8 7 4 2

Hint: If the mid-values of various classes are given in place of class intervals then these must first be converted into classes.

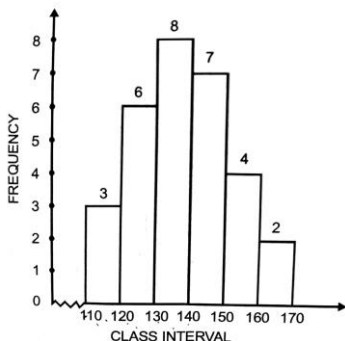


Fig. 2

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

A frequency polygon is another way of representing a given frequency distribution in graphic form. Frequency Polygons are more suitable than histograms if we wish to compare two or more frequency distributions.

A frequency polygon is constructed by first drawing the histogram and then joining the midpoints of the tops of the adjacent rectangles by straight lines. The mid points of both ends to the horizontal axis, resulting in a polygon.

A frequency polygon can also be constructed without first drawing the histogram. The frequency polygon is constructed by plotting each class frequency by drawing a dot (.) against its class mark and then connecting the successive dots with straight lines.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

A frequency polygon is another way of representing a given frequency distribution in graphic form. Frequency Polygons are more suitable than histograms if we wish to compare two or more frequency distributions.

A frequency polygon is constructed by first drawing the histogram and then joining the midpoints of the tops of the adjacent rectangles by straight lines. The mid points of both ends to the horizontal axis, resulting in a polygon.

A frequency polygon can also be constructed without first drawing the histogram. The frequency polygon is constructed by plotting each class frequency by drawing a dot (.) against its class mark and then connecting the successive dots with straight lines.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

A frequency polygon is another way of representing a given frequency distribution in graphic form. Frequency Polygons are more suitable than histograms if we wish to compare two or more frequency distributions.

A frequency polygon is constructed by first drawing the histogram and then joining the midpoints of the tops of the adjacent rectangles by straight lines. The mid points of both ends to the horizontal axis, resulting in a polygon.

A frequency polygon can also be constructed without first drawing the histogram. The frequency polygon is constructed by plotting each class frequency by drawing a dot (.) against its class mark and then connecting the successive dots with straight lines.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 3: Draw a frequency polygon for the following distribution of marks obtained by 50 students in an examination:

Marks Obtained:	10-20	20-30	30-40	40-50	50-60	60-70	70-80
No. of Students:	2	3	7	13	11	9	4
Marks Obtained:	80-90						
No. of Students:	01						

Solution: To construct the frequency polygon, we mark the frequency on the vertical axis and the values of the variable (i.e., marks) on the horizontal axis. Next, we construct the histogram representing the given frequency distribution and then join the mid points of the tops of the adjacent rectangles with straight lines to form a polygon.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 3: Draw a frequency polygon for the following distribution of marks obtained by 50 students in an examination:

Marks Obtained:	10-20	20-30	30-40	40-50	50-60	60-70	70-80
No. of Students:	2	3	7	13	11	9	4
Marks Obtained:	80-90						
No. of Students:	01						

Solution: To construct the frequency polygon, we mark the frequency on the vertical axis and the values of the variable (i.e., marks) on the horizontal axis. Next, we construct the histogram representing the given frequency distribution and then join the mid points of the tops of the adjacent rectangles with straight lines to form a polygon.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

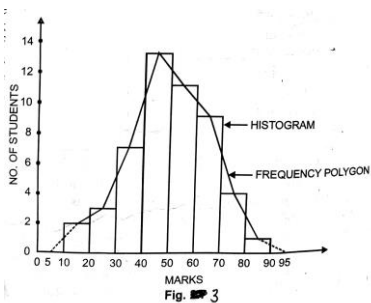
Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References



3.jpg

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 4: Draw a frequency polygon for the following distribution:

Class Interval: 15-25 25-35 35-45 45-55 55-65 65-75

Frequency: 10 16 18 15 13 4

Here the frequency polygon is constructed by plotting each class frequency by drawing a dot (.) against its class mark and the connecting the successive dots with straight lines.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 4: Draw a frequency polygon for the following distribution:

Class Interval: 15-25 25-35 35-45 45-55 55-65 65-75

Frequency: 10 16 18 15 13 4

Here the frequency polygon is constructed by plotting each class frequency by drawing a dot (.) against its class mark and the connecting the successive dots with straight lines.

Frequency Polygons

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

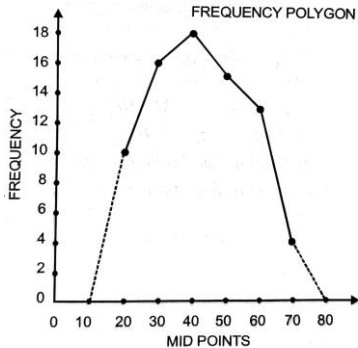
Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References



4.jpg les

Fig. 4

Frequency Curves

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

If the class intervals in a distribution are continuously reduced in size and if the no. of items in the distribution is continuously increased, the frequency polygon will resemble a smooth curve, called a smoothed frequency curve, or simply a frequency curve.

A frequency curves can be obtained from the histogram by joining the midpoints of the tops of the adjacent rectangles by a free hand.

Frequency Curves

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 5: Draw a frequency curves for the following distribution of marks obtained by 50 students in an examination:

Marks Obtained:	10-20	20-30	30-40	40-50	50-60	60-70	70-80
No. of Students:	2	3	7	13	11	9	4
Marks Obtained:	80-90						
No. of Students:	01						

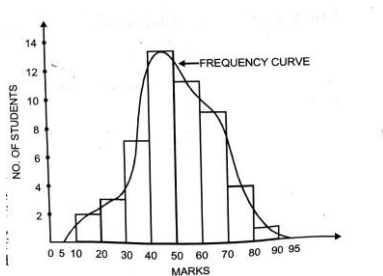


Fig. 2.9

5.jpg

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

An Ogive (pronounced oh-jive) is a graphic presentation of a cumulative frequency distribution. Since a cumulative frequency distribution can be of less than or more than type therefore there are two types of ogives viz., less than ogives or more than ogives.

Less than ogives: An ogive associated with a less than cumulative frequency is called less than ogives. A less than ogive is constructed by plotting points determined by the upper class boundary and the cumulative frequency of the individual classes and then connecting the successive points by a freehand curve. A less than ogive will be ascending.

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

An Ogive (pronounced oh-jive) is a graphic presentation of a cumulative frequency distribution. Since a cumulative frequency distribution can be of less than or more than type therefore there are two types of ogives viz., less than ogives or more than ogives.

Less than ogives: An ogive associated with a less than cumulative frequency is called less than ogives. A less than ogive is constructed by plotting points determined by the upper class boundary and the cumulative frequency of the individual classes and then connecting the successive points by a freehand curve. A less than ogive will be ascending.

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

More than ogives: An ogive associated with a more than cumulative frequency is called more than ogives. A more than ogive is constructed by plotting points determined by the lower class boundary and the cumulative frequency of the individual classes and then connecting the successive points by a freehand curve. A more than ogive will be descending.

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 6: The following data shows the marks obtained by 100 students in an examination:

Marks Obtained: 0-10 10-20 20-30 30-40 40-50 50-60

No. of Students: 10 9 25 30 10 16

(i) Construct a less than cumulative frequency distribution for the given data.

(ii) Construct a less than ogives of the cumulative frequency distribution of the given data.

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

SOLUTION (i) LESS THAN CUMULATIVE FREQUENCY DISTRIBUTION

Marks (Frequency)	No. of Students	Marks	No. of Students (Cumulative Frequency)
0 - 10	10	Less than 10	10
10 - 20	9	Less than 20	19
20 - 30	25	Less than 30	44
30 - 40	30	Less than 40	74
40 - 50	10	Less than 50	84
50 - 60	16	Less than 60	100

(ii) The "less than" ogive for the given data is shown in Fig. 2.10.

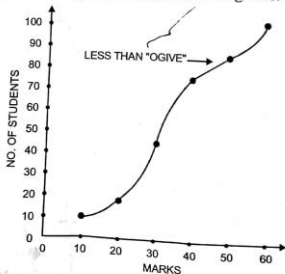


Fig. 2.10

6.jpg

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Example 7: Given below is the distribution of weights of a group of 60 students in a class:

Weights (in kg):	30-34	35-39	40-44	45-49	50-54	55-59
No. of Students:	03	5	12	18	14	06

Weights (in kg):	60-64
No. of Students:	02

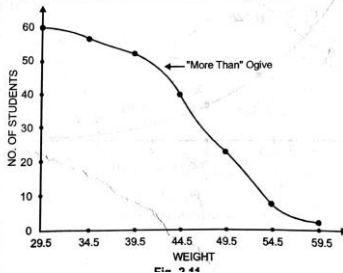
Draw a more than ogive for the above data.

SOLUTION. A "more than" ogive is determined by the lower class boundary and the cumulative frequency of the individual classes.

MORE THAN CUMULATIVE FREQUENCY DISTRIBUTION

Weight (in kg) (Class Boundary)	No. of Students	Weight	No. of Students (Cumulative Frequency)
29.5 - 34.5	3	More than 29.5	60
34.5 - 39.5	5	More than 34.5	57
39.5 - 44.5	12	More than 39.5	52
44.5 - 49.5	18	More than 44.5	40
49.5 - 54.5	14	More than 49.5	22
54.5 - 59.5	6	More than 54.5	8
59.5 - 64.5	2	More than 59.5	2

The "more than" ogive for the given data is shown in Fig. 2.11.



7.jpg

bibliography

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions




Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

-  J.K. Thukral, Business Statistics, Taxmann Publications Pvt. Ltd.
-  S.C. Gupta and V.K. Kapoor, Fundamentals of Statistics
-  K.P. Dhamu and K.Ramamoorthy, Fundamentals of Agricultural Statistics, Scientific Publishers (India), (2018).

Lecture 4

GLA
University
Mathura

Dr. Manoj
Kumar

Outline of
Lecture 4

Graphic
Presentations
of Frequency
Distributions

Histograms

Frequency
Polygons

Frequency
Curves

Ogives

References

Thanks !!!