

Linear Circuit Theory

L02: Nodal Analysis

- Solution of Question of last lecture
- Nodal Analysis with concepts of super node
- Concepts of dependent source
- Tutorial seat problems

Last lecture question:

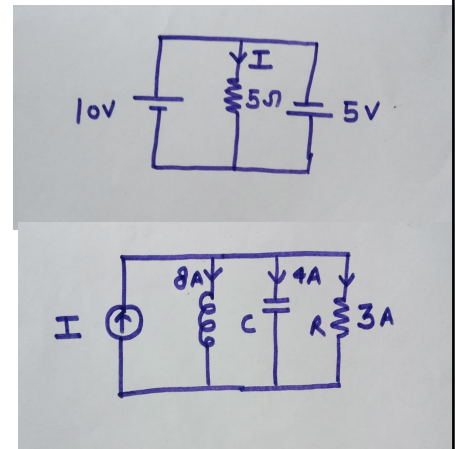
1. Which one have more resistance 1KW Heater or 2KW and why

Power is given by $P = \frac{V^2}{R}$, or $I^2 R$ but all appliance are made for parallel connection therefore Voltage is same and $P \propto \frac{1}{R}$. 1KW has more resistance then 2KW

2. Calculate the current in both the figure as shown

(a) 10 V and 5V are connect in parallel, circuit connection is not possible

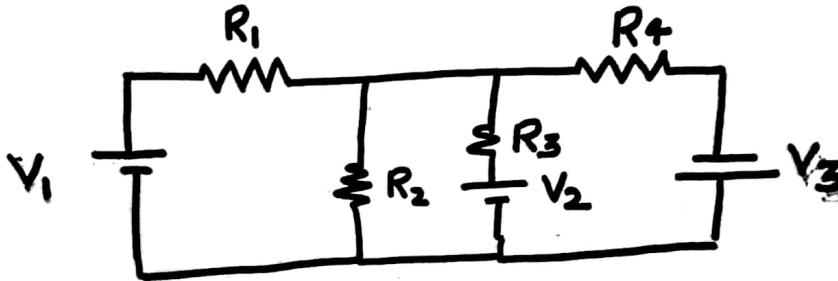
(b) Current $I = \sqrt{I_R^2 + (I_L^2 - I_C^2)}$ Ans=5A



Nodal Analysis (based on KCL)

Where nodal analysis required ?

*Number of node is minimum



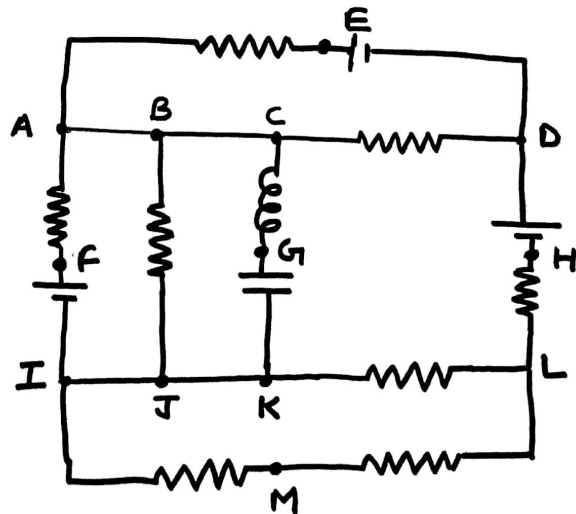
Ultimate aim to solve a problem with minimum effort

Nodal Analysis

Three basic rule to apply

1. Selection of node

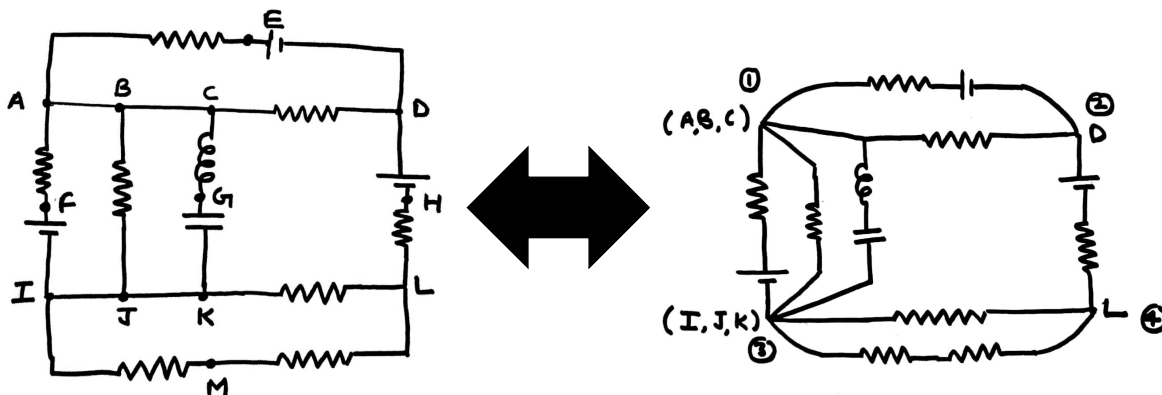
- Current same between the device
remove the node (F, G, H, M, E)
- If between two node, no elements or source consider single node (A, B, C) and (I, J, K)



(Ultimate purpose is to reduced the number of variable)

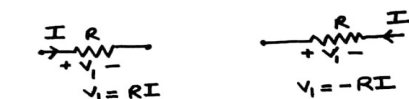
2. Assumption of node voltage

- Always consider one node as ground

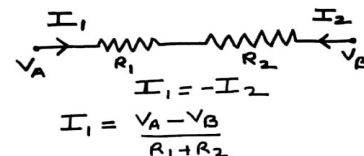


- Different Possible case of branch Current flow

a. Voltage current relation

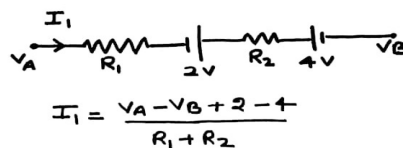


b. Current only with resistance



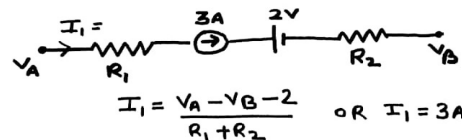
$$I_1 = \frac{V_A - V_B}{R_1 + R_2}$$

c. Current with voltage consideration



$$I_1 = \frac{V_A - V_B + 2 - 4}{R_1 + R_2}$$

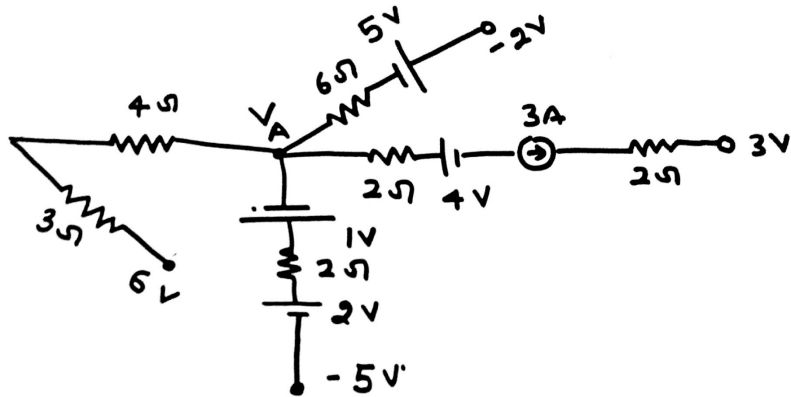
d. With current source



$$I_1 = \frac{V_A - V_B - 2}{R_1 + R_2} \quad \text{OR } I_1 = 3A$$

$$\text{OR } I_1 = \frac{V_A - V_B - 2}{R_1 + R_2} \pm 3$$

3. Apply
KCL

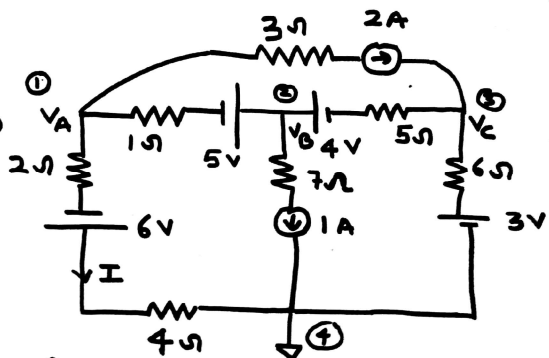


$$\frac{V_A - 6}{4 + 3} + \frac{V_A + 5 + 1 - 2}{2} + \frac{V_A + 2 + 5}{6} + 3 = 0$$

Numerical
Example

① NODE-1

$$\frac{V_A + 6}{2 + 4} + \frac{V_A - V_B + 5}{1} + 2 = 0$$



② NODE-2

$$\frac{V_B - V_A - 5}{1} + 1 + \frac{V_B - V_C - 4}{5} = 0$$

③ NODE-3

$$\frac{V_C - V_B + 4}{5} - 2 + \frac{V_C - 3}{6} = 0$$

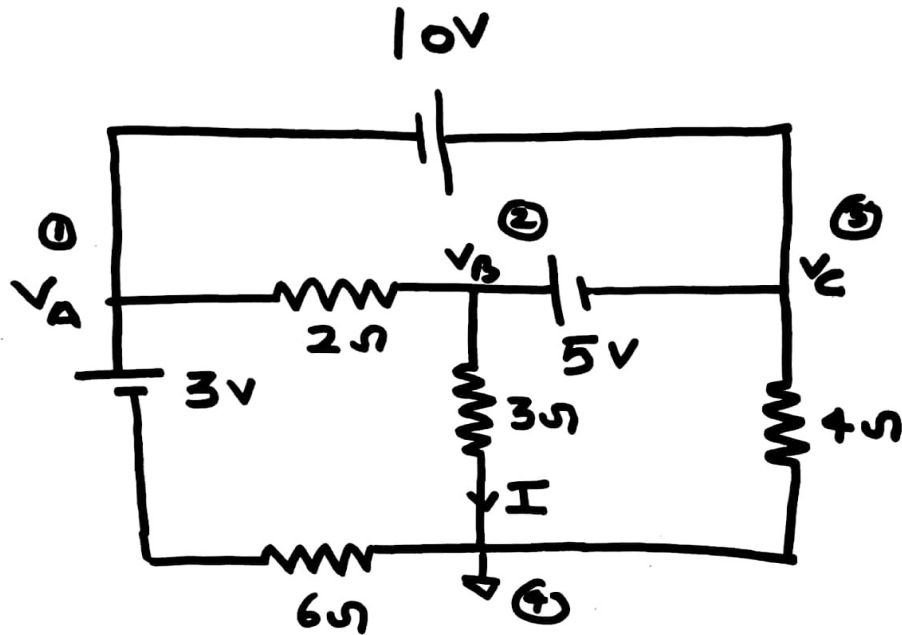
Super Node Analysis

@ KCL at

Node-1 ???

Node-2 ???

Node-3 ???



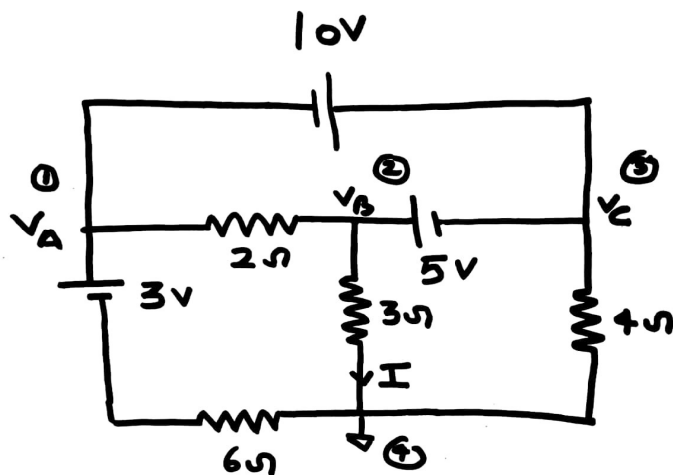
Method to solve the super node mesh problem

$$V_A - V_C = -10$$

$$V_B - V_C = 5$$

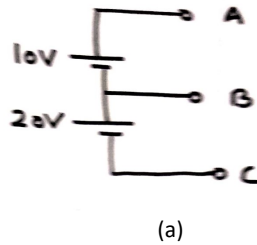
AT NODE-4

$$\frac{0 - V_A + 3}{6} + \frac{0 - V_B}{3} + \frac{0 - V_C}{4} = 0$$



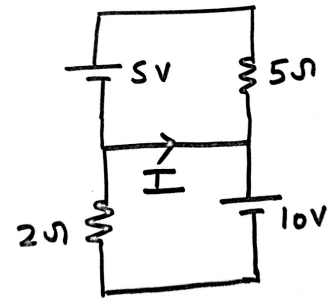
Tutorial basic question Seat

(a) Calculate value of V_A , V_B , V_C , V_{AB} , V_{BC} , V_{CA}



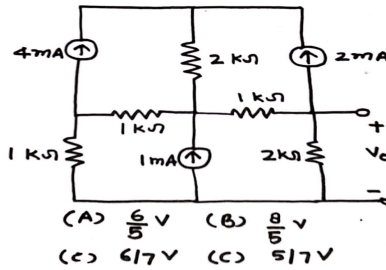
(b) Calculate I

(C) Calculate V_0

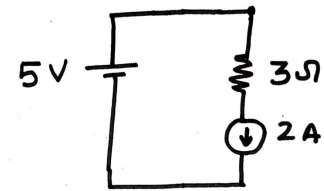


(b)

(b) Calculate Voltage across current source



(c)



(d)

In Next Lecture

- Answer of tutorial seat Problem
- Concepts of dependents source
- A seat of numerical examples

Thank you

